# Synthetic Struvite, $\mathrm{MgNH}_{4} \mathrm{PO}_{\mathbf{4}} \cdot \mathbf{6} \mathrm{H}_{\mathbf{2}} \mathrm{O}$ : Correct Polarity and Surface Features of Some Complementary Forms 

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#### Abstract

Struvite, $\mathrm{MgNH}_{4} \mathrm{PO}_{4} \cdot 6 \mathrm{H}_{2} \mathrm{O}, M_{r}=245 \cdot 4$, is orthorhombic, $P m n 2_{1}$. To establish the correct polarity, two refinements were completed from diffractometer Friedel-pair intensities measured with graphitemonochromatized $\mathrm{Cu} K \alpha$ radiation ( $\lambda=1.54178 \AA$ ) using two crystals grown under different, controlled, conditions: $\quad a=6.955(1), \quad b=6.142(1), \quad c=$ $11 \cdot 218$ (2) $\AA$ (average cell parameters obtained and refined from 20 reflexions, $55^{\circ} \leq 2 \theta \leq 110^{\circ}$ ), $\quad V=$ $479.2(1) \AA^{3}, Z=2, D_{x}=1.70 \mathrm{Mg} \mathrm{m}^{-3}, F(000)=260$, $\mu(\mathrm{Cu} K \alpha)=3.64 \mathrm{~mm}^{-1}$, room temperature. Final $R$ values for the correct and incorrect polarity were $0.0322,0.0402$ for the first crystal ( 764 reflexions, 723 Friedel pairs) and $0.0331,0.0419$ for the second crystal ( 863 reflexions, 805 Friedel pairs). These values, taken with the relative $F_{o}, F_{c}$ values of the Friedel pairs and with the results from a test proposed by Rogers [Acta Cryst. (1981), A37, 734-741], establish the correct polarity, identical for both crystals, at a very high confidence level. In order to complete a more accurate, room-temperature, determination, a third crystal was employed for graphite-monochromatized Mo $K \alpha$ diffractometry $(\lambda=0.71069 \AA)$ : $a=6 \cdot 966$ (1), $b=6 \cdot 142$ (1), $c=11 \cdot 217$ (2) $\AA$ (parameters from 24 reflexions, $22^{\circ} \leq 2 \theta \leq 43^{\circ}$ ), $V=$ 479.9 (1) $\AA^{3}, \quad D_{x}=1.70 \mathrm{Mg} \mathrm{m}^{-3}, \quad \mu($ Mo $K \alpha)=$ $0.40 \mathrm{~mm}^{-1}$. Final $R=0.0286$ for 989 independent reflexions. Within the chosen experimental conditions, the ammonium ion does not appear to be disordered contrary to the results from former investigations of struvite and the isomorphous arsenstruvite. The correct polarity has been correlated with crystal morphology and with surface features of some important complementary forms.


## Introduction

One of the aims of the present X-ray investigation of struvite was to establish its correct polarity, as yet unknown, which is indispensable for the unambiguous correlation of morphology and structure and for the correct interpretation of the morphologic modifications observed for this phosphate as a function of the supersaturation and pH for the mother
solutions. The knowledge of the polarity could therefore allow the interpretation of several experimental results (e.g. Abbona \& Boistelle, 1979; Wevers, Kars \& Schuiling, 1981). Besides, an accurate redetermination of the struvite structure might contribute to the understanding of the behaviour of the $\mathrm{NH}_{4}^{+}$ion. The more recent, and the only accurate, X-ray analysis of struvite, based on crystals of biological origin from a rather unusual source, supported the assumption of an ammonium ion rotating, possibly unevenly, around the $\mathrm{N} \cdots \mathrm{O}(1)$ direction, Fig. 2 [Whitaker \& Jeffery, 1970a, $b ; \mathrm{WJ}(a, b)$ hereinafter]. The situation around N in difference Fourier maps of the isomorphous arsenstruvite, $\mathrm{MgHN}_{4} \mathrm{AsO}_{4} \cdot 6 \mathrm{H}_{2} \mathrm{O}$, appeared similar to that found for struvite, but it was interpreted in terms of fractional occupancies of two H atoms in general positions with their symmetry equivalents related by the mirror plane orthogonal to the $x$ axis, giving altogether four atoms, including $\mathrm{H}(1)$, Fig. 2, around the special position occupied by N (Ferraris \& Franchini-Angela, 1973).

## Experimental

## Crystal habit

The crystals for the present analysis were prepared by mixing, without stirring, pure equimolar solutions $(0.05 M)$ of $\mathrm{MgSO}_{4} .7 \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{NH}_{4} \mathrm{H}_{2} \mathrm{PO}_{4}$; the initial pH's were obtained by adding, prior to mixing, appropriate volumes of 1.5 M ammonia to the $\mathrm{NH}_{4} \mathrm{H}_{2} \mathrm{PO}_{4}$ solution. Two crystals, to be employed for the polarity determination, were grown under the following initial conditions: crystal (1), $\beta=20, \mathrm{pH}=$ $6 \cdot 9,298 \mathrm{~K}$; crystal (2): $\beta=2 \cdot 8, \mathrm{pH}=6 \cdot 33,298 \mathrm{~K}$, where $\quad \beta=a\left(\mathrm{Mg}^{2+}\right) a\left(\mathrm{NH}_{3}\right) a\left(\mathrm{HPO}_{4}^{-}\right) / K_{\mathrm{sp}}$ (struvite) (for details and numerical values cf. Abbona, Lundager Madsen \& Boistelle, 1982). A third crystal, to be used for an accurate refinement, was grown at: $\beta=2 \cdot 5, \mathrm{pH}=6 \cdot 30,298 \mathrm{~K}$. In this way we operated within a large range of fairly high supersaturations. The variations in crystal habit complied with former results on this topic (Abbona \& Boistelle, 1979, and references therein). Special attention was paid to the relative extension of pedions $\{001\}$ and $\{00 \overline{1}\}$, particularly useful for controlling the crystal orientation
on the diffractometer. In this respect we may note that crystal (1) showed $\{001\}$ well developed and $\{00 \overline{\bar{l}}\}$ much less extended, crystal (2) showed $\{001\}$ moderately developed whilst the complementary form was missing, crystal (3) showed $\{001\}$ well developed and $\{00 \overline{1}\}$ very small; the other forms in order of decreasing importance were: $\{011\},\{101\},\{01 \overline{2}\},\{0 \overline{1}\}$. Fig. 1 shows the forms of crystal (3) indexed according to the correct polarity.

## Diffractometer measurements

Crystals (1) and (2) were employed for the measurements of an adequate number of Friedel pairs with a Nicolet $R 3$ diffractometer using $\mathrm{Cu} K \alpha$ radiation. To perform a more accurate refinement, Mo $K \alpha$ radiation was used with crystal (3) to collect a large number of independent reflexions. In all three cases the $\omega$-scan technique was employed at variable speed; from $1.5^{\circ} \mathrm{min}^{-1}$ for the weakest to $10 \cdot 0^{\circ} \mathrm{min}^{-1}$ for the strongest reflexions; scan range: $1.60^{\circ}$; left and right backgrounds measured in stationary mode for 0.8 times the peak-scan time. Two standard reflexions, monitored every fiftieth measurement: no decrease in the course of the measurement. Crystal (1): $0.20 \times$ $0.12 \times 0.32 \mathrm{~mm}$, reciprocal-sphere octants $h k l$ and $h k \bar{l}$ explored within $2 \theta=125^{\circ} ; 771$ reflexions measured, 767 with $I \geq 2 \sigma(I)$ considered as observed and included in the analysis ( $h: 0-8 ; k: 0-7 ; l:-12-+12$ ); 3 low-angle reflexions discarded in the course of the refinement because they were probably affected by the secondary-extinction effect. 723 Friedel pairs. Crystal (2): $0.28 \times 0.18 \times 0.41 \mathrm{~mm}$, octants $h k l$ and $h k \bar{l}$ explored within $2 \theta=130^{\circ} ; 879$ reflexions obtained, 872 observed; 820 Friedel pairs ( $h: 0-8 ; k: 0-7$; $l:-13-+13)$; Cu attenuator inserted for 19 intensities exceeding 60000 counts s ${ }^{-1}$ on the pre-scan and 9 of these still had to be discarded because of poor $F_{o}$ vs $F_{c}$ agreement. Empirical absorption correction, based on the $\psi$-scan method (North, Phillips \& Mathews, 1968) and four reflexions, $48^{\circ} \leq 2 \theta \leq 98^{\circ}$; absorption coefficients 1.00 to $1 \cdot 20$. Crystal (3): $0.20 \times 0.30 \times$ $0.45 \mathrm{~mm}, h k \bar{l}$ octant explored within $2 \theta=70^{\circ} ; 1034$ independent reflexions measured, 990 observed ( $h: 1-$ $8 ; k: 0-9 ; I: \overline{18}-0$ ). Only reflexion 004 had to be discarded. Absorption correction based on the $\psi$-scan method and four reflexions, $10 \cdot 7^{\circ} \leq 2 \theta \leq 35 \cdot 7^{\circ}$; coefficients $1 \cdot 005$ to $1 / 143$.


Fig. 1. Clinographic projecton of the forms of crystal (3) indexed according to the correct polarity.

## Refinement and determination of the correct polarity

For all subsequent computations use was made of the SHELXTL system (Sheldrick, 1981). The coordinates of the non-hydrogen atoms obtained by $\mathrm{WJ}(a)$ were used as a starting model for the refinement based on standard least-squares methods. The H atoms were located on difference Fourier maps at an advanced stage of the anisotropic refinement (see Results). The scattering factors for neutral atoms were taken from International Tables for X-ray Crystallography (1974) and the anomalous-dispersion corrections for $\mathrm{O}, \mathrm{N}$, and Mg were introduced from the beginning. The origin was fixed by keeping constant, at 0.0005 , the $z$ coordinate of P . The positional parameters of the H atoms were refined under the following initial constraints using three different 'free variables' (Sheldrick, 1981). The N-H lengths were set equal to $0.88 \pm 0.005 \AA$, FVAR1, and the $\mathrm{H} \cdots \mathrm{H}$ separations equal to FVAR $1 \times 1.633 \pm 0.005 \AA$ in order to ensure a tetrahedral arrangement around the N atom. The $W-\mathrm{H}(i, j)$ and $\mathrm{H}(i, 1) \cdots \mathrm{H}(i, 2)$ distances were similarly constrained to refine from $0.95 \pm 0.005 \AA$, FVAR2, and $1.48 \pm 0.010 \AA$, FVAR3, with no constraint between them to allow for more latitude of settlement. These starting values looked sensible and agree with those reported in the literature. The thermal parameters of the H atoms were set equal to 1.2 times the equivalent $U$ values of the bonded atoms. In the case of crystal (2) unit weights proved satisfactory; in the final cycles of the other two refinements the following weighting scheme was introduced: $w=$ $1 /\left[\sigma^{2}\left(F_{o}\right)+G F_{o}^{2}\right]$ where $\sigma$ is the standard deviation of $F_{o}$, based on counting statistics, and $G$ a variable to be adjusted after each cycle. Under the above conditions two parallel refinements were run with the data of both crystals (1) and (2): one based on the set of coordinates from $\mathrm{WJ}(a)$ and the other on the antipodal $1-x, 1-y, 1-z$ set (Sheldrick, 1981). At convergence (mean $\Delta / \sigma<0.04$ ) the following values of the agreement parameters were obtained for the former and latter set of coordinates respectively. Crystal (1): $R=0.0402,0.0322 ; ~ w R=0.0458,0.0332$; $R G=0.0596,0.0430$; goodness of fit $=2 \cdot 283,1 \cdot 224$; $G=0.00065,0.00126$ for 764 reflexions and 98 parameters. FVARI $=0.90(3), 0.89(2) ;$ FVAR2 $=0.86(2)$, 0.87 (2); $\quad$ FVAR $3=1.37$ (4), $\quad$ I.39 (3) $\AA . \quad$ Crystal (2): $R=0.0419,0.0331 ; R G=0.0468,0.0378$; goodness of fit $=0.798,0.634$ for 863 reflexions and 79 parameters; the coordinates of the H atoms of the water molecules were kept fixed in the closing cycles. FVAR1 $=0.91(2), \quad 0.92(2) ; \quad$ FVAR2 $=0.812(4)$, $0.812(4) ;$ FVAR $3=1.351(6), 1 \cdot 351$ (6).

The Hamilton test (International Tables, 1974; pp. 287-292; Rogers, 1981) favours the second polarity at the 0.005 confidence level and the scrutiny of the relative $F_{o}, F_{c}$ values of the Friedel pairs confirms the choice. Besides, Rogers's (1981) parameter (see

Calleri, Gavetti, Ivaldi \& Rubbo, 1984) refined to $\pm 1.06$ (7) for the correct and incorrect polarity respectively. Therefore, the correct polarity of struvite may be considered as established at a very high reliability level. With reference to the triad of axes of Figs. 1 and 2 and to that of $\mathrm{WJ}(a)$, the correct coordinates are those given in Table 1, obtained from the refinement based on the data collected with crystal (3). This third refinement was completed under the above conditions excepting that FVAR3 was set equal to $1.48 \pm$ $0.005 \AA$. The correct and antipodal set of coordinates yielded at convergence (mean $\Delta / \sigma \leq 0 \cdot 01$ ) the following values. Crystal (3): $R=0.0286,0.0282 ; w R=$ $0.0302,0.0297 ; R G=0.0364,0.0357$; goodness of fit $=1 \cdot 132,1 \cdot 127 ; G=0.00062,0.00059$ for 989 independent reflexions and 98 parameters; FVARI = $0.92(2), \quad 0.92(2) ; \quad$ FVAR2 $=0.80(1), \quad 0.80(1)$; FVAR3 $=1.34(2), 1 \cdot 34$ (2) $\AA$. Here the deductions derivable from the $R$ ratio are inconclusive (Rogers, 1981).*

## Results

Tables 1 and 2 give the final parameters and relevant distances and angles obtained from the more accurate ( $R=0.0286$ ) third refinement using the coordinates for the correct polarity previously established. There is no significant difference between bond distances and angles based on the two sets of coordinates in all three cases. The values obtained from the refinements based on $\mathrm{Cu} K \alpha$ diffractometry do not differ from those of Table 2 by more than two or three times the e.s.d.'s there reported. $\dagger$ The mean values of Table 2 are unweighted and the bond distances are uncorrected for the libration effect; at any rate the in-phase libration corrections were not significant. For a detailed description of the structure and its hydrogenbonding net, the reader is referred to $\mathrm{WJ}(a)$.

All H atoms were located on difference Fourier maps and in the case of the third refinement the heights of the peaks corresponding to the H atoms of the water molecules ranged from 0.54 to $0.45 \mathrm{e}^{\AA^{-3}}$. The distribution of residual electron density around N was neat and showed two peaks [ $\mathrm{H}(1) 0.44$ and $\left.\mathrm{H}(2) 0.34 \mathrm{e} \AA^{-3}\right]$, coplanar with N , on the mirror plane orthogonal to the $x$ axis, and two others in general positions related by the mirror plane itself [ $\mathrm{H}(3)$ $0 \cdot 35 \mathrm{e}^{\AA^{-3}}$ ] as it obtains with the phosphate-group O

[^0]Table 1. Atomic coordinates ( $\times 10^{4}$ for non-hydrogen atoms, $\times 10^{3}$ for hydrogen atoms) and isotropic temperature factors ( $\AA^{2} \times 10^{4}$ ), with e.s.d.'s in parentheses

|  | $x$ | $y$ | $z$ | $U_{\text {eq }}^{*}$ or $U_{\text {iso }}$ |
| :---: | :---: | :---: | :---: | :---: |
| P | 10000 | 10065 (1) | 10005 | 143 (1)* |
| $\mathrm{O}(1)$ | 10000 | 10220 (3) | 1378 (2) | 226 (5)* |
| $\mathrm{O}(2)$ | 10000 | 2380 (2) | 9465 (2) | 218 (5)* |
| O(3) | 8179 (2) | 8863 (2) | 9584 (1) | 211 (3)* |
| Mg | 10000 | 6232 (1) | 6283 (1) | 176 (2)* |
| $W(1)$ | 10000 | 3163 (3) | 7137 (2) | 376 (8)* |
| H(1,1) | 1000 | 305 (7) | 785 (4) | 449 |
| H(1, 2) | 1000 | 184 (7) | 685 (4) | 449 |
| $W(2)$ | 10000 | 9214 (4) | 5356 (3) | 406 (8)* |
| H(2, 1) | 897 (5) | 986 (4) | 503 (4) | 489 |
| $W(3)$ | 7825 (3) | 7369 (2) | 7382 (1) | 265 (4)* |
| H(3, 1) | 815 (5) | 795 (4) | 806 (3) | 319 |
| H(3, 2) | 720 (4) | 815 (5) | 702 (3) | 319 |
| $W(4)$ | 7892 (2) | 5147 (2) | 5148 (2) | 321 (5)* |
| H(4, 1) | 768 (5) | 387 (2) | 512 (3) | 385 |
| $\mathrm{H}(4,2)$ | 702 (4) | 590 (3) | 493 (3) | 385 |
| N | 10000 | 6341 (5) | 2673 (3) | 332 (8)* |
| $\mathrm{H}(1)$ | 1000 | 761 (3) | 224 (3) | 397 |
| H(2) | 1000 | 666 (5) | 348 (2) | 397 |
| H(3) | 895 (3) | 551 (3) | 248 (2) | 397 |

* $U_{e q}$ is defined as one third of the trace of the orthogonalized $U_{i j}$ tensor.
atoms (Fig. 2, Table 2). This model refined smoothly and the final difference map showed no ripples, except those associated with P and Mg (height $\sim 0.25 \mathrm{e} \AA^{-3}$ ). The refinements based on $\mathrm{Cu} K \alpha$ diffractometry yielded similar results. Hence, within the chosen experimental conditions, the postulate of disorder for the ammonium ion does not seem necessary, contrary to the findings of $\mathrm{WJ}(a, b)$. The ion is in the form of a fairly regular tetrahedron. The $\mathrm{PO}_{4}$ tetrahedron is remarkably regular (Table 2 ) and reveals an appreciable $\pi$-bond character equally divided among the four bonds (e.g. Calleri \& Speakman, 1964, and references therein).


Fig. 2. Projection of the unit-cell contents along [010].

## Table 2. Bond lengths ( $\AA$ ) and angles ( ${ }^{\circ}$ )

| Phosphate tetrahedron; e.s.d.'s in parentheses |  |  |  | Mg. $6 \mathrm{H}_{2} \mathrm{O}$ octahedron; e.s.d.'s in parentheses |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}-\mathrm{O}(1)$ | 1.543 (2) | $\mathrm{O}(1)-\mathrm{P}-\mathrm{O}(2)$ | $109 \cdot 5(1)$ | $\mathrm{Mg}-W(1)$ | 2.115(1) | $W(1)-\mathrm{Mg}-W(3)$ | 91.8(1) |
| $\mathrm{P}-\mathrm{O}(2)$ | 1.546 (2) | $\mathrm{O}(1)-\mathrm{P}-\mathrm{O}(3)$ | $109 \cdot 6$ (1) | $\mathrm{Mg}-W(2)$ | 2.106 (3) | $W(1)-\mathrm{Mg}-W(4)$ | 89.5 (1) |
| $\mathrm{P}-\mathrm{O}(3)$ | 1.542 (1) | $\mathrm{O}(2)-\mathrm{P}-\mathrm{O}(3)$ | 108.7 (1) | $\mathrm{Mg}-W(3)$ | 2.075 (2) | $W(2)-\mathrm{Mg}-W(3)$ | 90.0 (1) |
| Mean | 1.544 (1) | $\mathrm{O}(3)-\mathrm{P}-\mathrm{O}\left(3^{\text {i }}\right.$ ) | 110.7 (1) | $\mathrm{Mg}-W(4)$ | 2.054 (2) | $W(2)-\mathrm{Mg}-W(4)$ | 88.6 (1) |
|  |  | Mean | 109.6(1) | Mean | 2.087 (2) | $W(3)-\mathrm{Mg}-W\left(3^{1}\right)$ | 93.8 (1) |
| $\mathrm{O}(1)-\mathrm{O}(2)$ | 2.523 (3) |  |  |  |  | $W(3)-\mathrm{Mg}-W(4)$ | 87.4 (1) |
| $\mathrm{O}(1)-\mathrm{O}(3)$ | $2 \cdot 521$ (2) |  |  | $W(1)-W(3)$ | 3.007 (3) | $W(4)-\mathrm{Mg}-W\left(4^{1}\right)$ | 91.3(1) |
| $\mathrm{O}(2)-\mathrm{O}(3)$ | 2.509 (2) |  |  | $W(1)-W(4)$ | 2.935 (3) | Mean | $90 \cdot 3$ (1) |
| $\mathrm{O}(3)-\mathrm{O}\left(3^{\text {i }}\right.$ ) | $2 \cdot 537$ (3) |  |  | $W(2)-W(3)$ | 2.957 (3) |  |  |
| Mean | $2 \cdot 522$ (2) |  |  | $W(2)-W(4)$ | 2.907 (3) |  |  |
|  |  |  |  | $W(3)-W\left(3^{1}\right)$ | 3.030 (3) |  |  |
|  |  |  |  | $W(3)-W(4)$ | 2.853 (2) |  |  |
|  |  |  |  | $W(4)-W\left(4^{1}\right)$ | 2.936 (3) |  |  |
|  |  |  |  | Mean | 2.946 (1) |  |  |

Hydrogen-bonding scheme; e.s.d.'s are $0.002-0.003 \AA$ and $0.1^{\circ}$ for distances and angles between O atoms, $0.02-0.04 \AA$ and $1^{\circ}-4^{\circ}$ for distances and angles involving H atoms

| A | $B$ | C | D | $E$ | $A B$ | BC | $A C$ | $C E$ | $C D$ | DE | $B C D$ | $A B C$ | $C D E$ | ACE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{O}(2)$ | $\cdots \mathrm{H}(1,1)$ | $W(1)$ | 1,2) | $W\left(2^{\text {ii }}\right.$ ) | 1.85 | 0.81 | 2.655 | 3.144 | $0 \cdot 87$ | $2 \cdot 33$ | 106 | 172 | 155 |  |
| $\mathrm{O}\left(3^{\text {iii }}\right)$ | $\cdots \mathrm{H}(2,1)$ | W(2) | (2,1) | (3iv) | 1.76 | 0.90 | 2.656 | 2.656 | 0.90 | 1.76 | 106 | 172 | 172 | $113 \cdot 0$ |
| $\mathrm{O}(3)$ | $\cdots \mathrm{H}(3,1)$ | $W$ (3) | 3,2) | $\left(1^{v}\right.$ ) | 1.80 | 0.87 | 2.646 | 2.708 | 0.77 | 1.97 | 110 | 164 | 163 | $105 \cdot 4$ |
| $\mathrm{O}\left(3^{\text {vi }}\right.$ ) | $\cdots \mathrm{H}(4,1)$ | V(4) | 4,2) | $\left(2^{\text {vii }}\right.$ ) | 1.88 | 0.80 | 2.651 | $2 \cdot 637$ | $0 \cdot 80$ | 1.84 | 114 | 161 | 178 | 104.5 |
| $W\left(3^{\text {viii }}\right.$ ) | $\cdots \mathrm{H}(3)$ |  |  |  | $2 \cdot 16$ | 0.92 | 3.028 |  |  |  | 110 | 157 |  | 125.9 |
| $W\left(4^{\text {i }}\right.$ ) | $\cdots \mathrm{H}(2)$ |  | O(1) |  | $2 \cdot 56$ | $0 \cdot 92$ | $3 \cdot 226$ | $2 \cdot 790$ | 0.92 | 1.87 | 110 | 130 | 179 |  |

Superscripts refer to the equivalent positions: (i) $2-x, y, z$; (ii) $x, y-1, z$; (iii) $1 \cdot 5-x, 2-y, z-0 \cdot 5$; (iv) $0.5+x, 2-y, z-0.5$; (v) $0.5+x, 2-y, 0 \cdot 5+z$; (vi) $1.5-x, 1-y, z-0.5$; (vii) $x-0.5,1-y, 0.5+z$; (viii) $0.5-x, 1-y, z-0.5$.

## Discussion

## Behaviour of $\mathrm{NH}_{4}^{+}$; electrostatic balance

Three of the H atoms of this group, $\mathrm{H}(1), \mathrm{H}(3)$ and $\mathrm{H}\left(3^{i}\right)$, form hydrogen bonds (Table 2). The fourth, $\mathrm{H}(2)$, is $2 \cdot 56(3) \AA$ from $W(4)$ and $W\left(4^{\mathrm{i}}\right)$ and the corresponding $W-H \cdots N$ angles are $130(2)^{\circ}$; therefore, these interactions cannot be considered true hydrogen bonds, but contribute to clamping in position the ammonium ion and to achieving electrostatic balance. Within the first coordination sphere the ion is surrounded by five O atoms: $\mathrm{O}(1), W(3), W\left(3^{i}\right)$ and, at larger distances, $W(4), W\left(4^{1}\right)$. The coordination is then strictly reminiscent of that of $\mathrm{K}^{+}$in the struvite analogue $\mathrm{MgKPO}_{4} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (Mathew \& Schroeder, 1979). The coordination cavity is a very prolate spheroid. It may be noted that a range of $\mathrm{N} \cdots \mathrm{O}$ distances ( $2 \cdot 79-3 \cdot 23 \AA$, Table 2 ) meets coordination number (CN) 5 according to the survey by Khan \& Baur (1972). A small CN (from 4 to 5) in its turn favours the hydrogen-bonding tendency of $\mathrm{NH}_{4}^{+}$ to prevail over its pseudo-alkali character displayed with large CN (7 to 9). All this agrees with an ordered configuration of this group.

The electrostatic balance, calculated exploiting the Brown \& Shannon (1973) relationships with appropriate parameters, shows that $\mathrm{O}(1)$ and $W(2)$ are underbalanced to the same extent ( $\sum s_{i}=1.86$ instead of $2 \cdot 00$ ). However, the underbonding of $\mathrm{O}(1)$ agrees with the tendency for $\mathrm{NH}_{4}^{+}$ions with small CN 's to be bonded to slightly undersaturated O anions (Khan \&

Baur, 1972), whilst $W(2)$ may receive a small further contribution from $\mathrm{NH}_{4}^{+}$[Fig. 2; $W(2) \cdots \mathrm{H}(2)=$ $2 \cdot 63$ (3) $\left.\AA, W(2) \cdots \mathrm{H}(2)-\mathrm{N}=155(2)^{\circ}\right]$. The detailed results have been deposited.

## Surface features and growth rates

The correct polarity being known, the more likely surface structures of any form of struvite crystals can be deduced applying the Hartman \& Perdok (1955) periodic bond chain (PBC) method [ $c f$. also the preceding paper on epsomite (Calleri et al., 1984). The outstanding morphologic zone of struvite crystals is [100]; Fig. 3 is the projection of the structure along this axis. It displays the shape of the most likely among the PBC's which can be singled out along [100] and shows the surface structures of the common forms $\{001\},\{011\},\{01 \overline{2}\}$ and of their complementary ones. The PBC chosen by us along [100] can be connected to its symmetry equivalent along [010] and [ $01 \overline{1} 1$, which are also PBC directions (Abbona \& Boistelle, 1979), to yield slices of thickness $d_{002}$ and $d_{011}$ respectively. The faces of $\{001\}$ and $\{011\}$, of type $F$ after Hartman \& Perdok (1955), are more developed than those of the complementary $\{00 \overline{1}\}$ and $\{0 \overline{1} \overline{1}\}$ forms as we could clearly notice on our crystals. The effect is due to the different growth rates of the opposite faces relatable to their different surface structures. In fact, at the outermost layers of (001) and ( 011 ), Fig. 3, there is a higher density of electropositive groups $\left(\mathrm{NH}_{4}, \mathrm{H}\right)$ than at the layers of $(00 \overline{\mathrm{I}})$
and $(0 \overline{1} \overline{1})$ where a higher density of $\mathrm{PO}_{4}$ groups obtains. This implies different activation energies for the desorption and desolvation processes from the opposite faces and consequently a different extension. The above effect may be strengthened or attenuated by the different electronic polarizability of the complementary surfaces (Monier \& Kern, 1956, and references therein). Monier \& Kern's (1956) theory, originally developed for growth in the gaseous state of noncentrosymmetric crystals, leads to the conclusion that the more polarizable of two complementary forms is the more favoured. The theory seems to hold its validity also in the present case of growth from solution, with all due reserve (e.g. Cadoret, 1965). In point of fact, only $\mathrm{NH}_{4}$ groups outcrop on (001) and they are likely to be more polarizable than the $\mathrm{PO}_{4}$ and $\mathrm{Mg}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}$ groups emerging on $(00 \overline{1})$, Fig. 3. Nonetheless this contribution should become determinant only when the difference between the activation energies of depolarization of two complementary forms [ $\Delta P \simeq 4 \mathrm{~kJ} \mathrm{~mol}^{-1}$, as calculated by Cadoret (1965) and Cadoret \& Monier (1967) for some ionic compounds] is greater than the corresponding difference between the dehydration or surface diffusion activation energies per bonding unit. The lack of calculated or experimental values does not allow us to draw semiquantitative conclusions on the effective role played by the surface depolarization on the relative development of complementary forms.

Form $\{01 \overline{2}\}$ is usually well developed whilst its complementary $\{0 \overline{\mathrm{I}} 2\}$ is never present. The stability of the former, which has an $S$ character, may be accounted for on postulating a selective absorption


Fig. 3. Projection along [ $\overline{1} 00]$ of the structure. The profiles of the more common forms are displayed. The more likely [100] PBC is sketched inside.
of some component from the mother solution on the steps of $S$ profile (Cadoret, 1965).

It is necessary to emphasize that changes in the growth conditions, such as impurity concentration, pH , supersaturation, may even invert the relative size of faces belonging to the same pair of complementary forms (Cadoret \& Monier, 1965). In the specific instance of struvite, crystals from the same natural source were found to exhibit different developments of ( 001 ) and ( $00 \overline{1}$ ) with size inversion (Kalkowsky, 1886). This may explain why arsenstruvite (Ferraris \& Franchini-Angela, 1973) was found to show a polarity opposite to that found here for struvite. The arsenstruvite crystals were prepared (De Schulten, 1903) from solutions much more concentrated and acidic than ours; besides, they were rich in foreign ions ( $\left[\mathrm{Na}^{+}\right] \simeq 0.6 \mathrm{M}$ ) and non-stoichiometric ([As] $\simeq$ $1.5[\mathrm{Mg}])$. These marked differences in the growth conditions affected the arsenstruvite crystal habit which is different from ours, being tabular according to $\{010\}$, with small $\{001\},\{012\},\{011\}$ and $\{110\}$ (Ferraris \& Franchini-Angela, 1973). In conclusion, the crystal habit alone is not always a sufficient criterion for controlling the correct polarity of struvite. Other surface or bulk effects, such as etch pits and pyroelectricity respectively, are to be considered; research on this subject is in progress.

## References

Abbona, F. \& Boistelle, R. (1979). J. Cryst. Growth, 46, 339-354. Abbona, F., Lundager Madsen, H. E. \& Boistelle, R. (1982). J. Cryst. Growth, 54, 6-14.

BROWN, I. D. \& SHANNON, R. D. (1973). Acta Cryst. A29, 266-282.
Cadoret, R. (1965). Dr Phys. thesis, Caen Univ.
Cadoret, R. \& Monier, J. P. (1965). Adsorption et Croissance Cristalline. Paris: CNRS.
Cadoret, R. \& Monier, J. P. (1967). J. Cryst. Growth, 1, 59-66.
Calleri, M., Gavetti, A., Ivaldi, G. \& Rubbo, M. (1984). Acta Cryst. B40, 218-222.
Calleri, M. \& Speakman, J. C. S. (1964). Acta Cryst. 17, 10971103.

De Schulten, M. R. (1903). Bull. Soc. Fr. Minéral. 26, 95-98.
Ferraris, G. \& Franchini-Angela, M. (1973). Acta Cryst. B29, 859-863.
Hartman, P. \& Perdok, W. G. (1955). Acta Cryst. 8, 49-52, 521-524, 525-529.
International Tables for X-ray Crystallography (1974). Vol. IV. Birmingham: Kynoch Press.
Kalkowsky, E. (1886). Z. Kristallogr. 11, 1-4.
Khan, A. A. \& Baur, W. H. (1972). Acta Cryst. B28, 683-693.
Mathew, M. \& Schroeder, L. W. (1979). Acta Cryst. B25, 11-13.
Monier, J. C. \& Kern, R. (1956). Bull. Soc. Fr. Minéral. Cristallogr. 79, 455-514.
North, A. C. T., Phillips, D. C. \& Mathews, F. S. (1968). Acta Cryst. A24, 351-359.
Rogers, D. (1981). Acta Cryst. A37, 734-741.
Sheldrick, G. M. (1981). SHELXTL. An Integrated System jor Solving Refining and Displaying Crystal Structures from Diffraction Data (3rd revision). Univ. of Göttingen.
Wevers, M. A. R., Kars, H. \& Schuiling, R. D. (1981). Bull. Soc. Fr. Minéral. Cristallogr. 104, 686-689.
Whitaker, A. \& Jeffery, J. W. (1970a). Acta Cryst. B26, 14291440.

Whitaker, A. \& Jeffery, J. W. (1970b). Acta Cryst. B26, 14401444.


[^0]:    *Lists of structure factors and anisotropic thermal parameters and the results for the electrostatic balance have been deposited with the British Library Lending Division as Supplementary Publication No. SUP39141 (10pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CHI 2HU, England.
    $\dagger$ The results from the two refinements based on $\mathrm{Cu} K \alpha$ diffractometry are available from the authors.

